

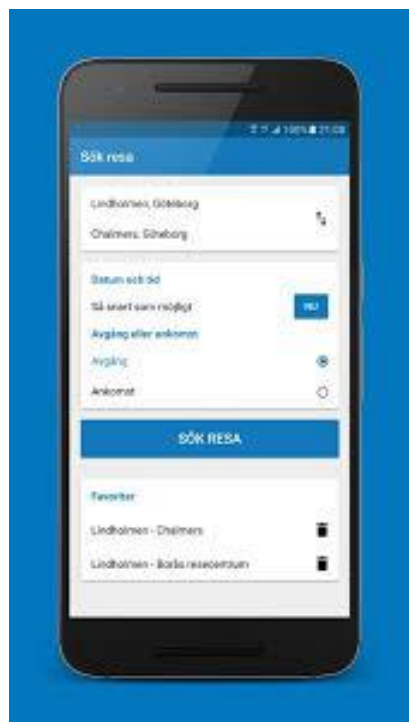
# Algorithms

Birgit Grohe

2019-11-06



# Used an Algorithm Today?



Reseplaneraren - Västtrafik

http://www.vasttrafik.se/sv/Att-resa/Reseplaneraren/?from=&to=020051701- RSS - Google

Sajtarna | English

**västtrafik** Startside Att resa Trafikläget Priser & Kort Om Västtrafik Aktuellt Kontakta oss Mina sidor

Att resa / Reseplaneraren

**Att resa**  
 Heltrafik  
 Kompletterings trafik  
 Ledsagarservice  
 Linjenäts- & hållplatskartor  
 Mobila tjänster  
 Närtrafik  
 Omlottzoner  
 Pendelparkering  
 Resa med barnvagn  
 Resa med Swebus Express  
 Resa med tåg  
 Resa vidare  
 Resegaranti  
 Reseplaneraren  
 Avstånd från hållplats  
 Alternativt genvägar  
 Reserare på din sida  
 Har du någonting som inte fungerar?  
 Har du någonting som inte fungerar?

**Reseplaneraren**

Sökt resa: Korsvägen, GÖTEBORG (Hållplats) - Opalatorget, GÖTEBORG (Hållplats) (torsdag 16 oktober 2008)

Ny sökning | Ändra sökning

Avgång	Ankomst	Restid	Bytan	Trafikslag
<input type="checkbox"/> 17:50	18:19	00:29	1	Spårvagn 8, Spårvagn 7
<input checked="" type="checkbox"/> 17:59	18:28	00:29	1	Spårvagn 8, Spårvagn 7
<input type="checkbox"/> 18:08	18:38	00:30	1	Spårvagn 8, Spårvagn 7
<input type="checkbox"/> 18:25	18:49	00:24	0	Spårvagn 8
<input type="checkbox"/> 18:31	19:02	00:31	1	Spårvagn 6, Spårvagn 7
<input type="checkbox"/> 18:35	19:07	00:32	1	Spårvagn 8, Spårvagn 1

Returresa << Tillbaka resor | Senare resor >>

Detaljerad resväg | Besöka som text | Mellanliggande hållplatser | Skicka till e-post | Skriv ut resor

Detaljerad resväg: Korsvägen - Opalatorget (torsdag 16 oktober 2008)

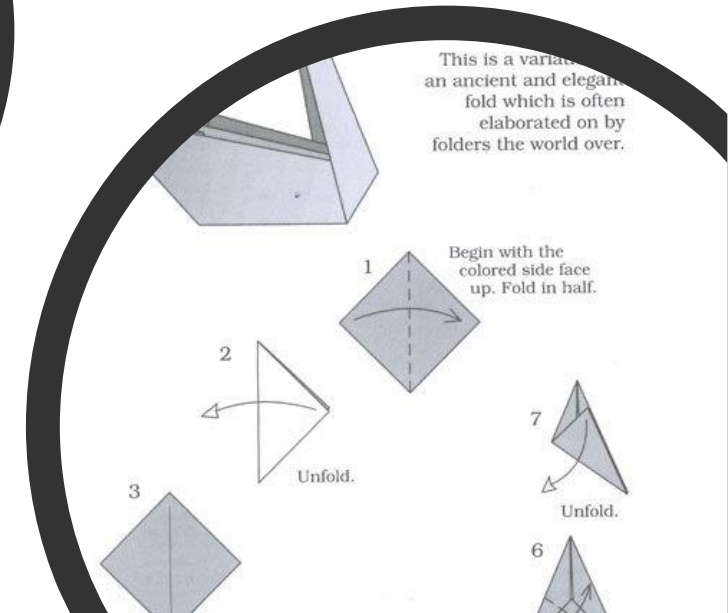
Linje	Från/Till	Tid	Information
Spårvagn 8	Korsvägen Läge F Frölunda Torg Läge B	Avg: 17:59 Ank: 18:19	Mot: Frölunda Torg
Spårvagn 7	Frölunda Torg Läge B Opalatorget Läge B	Avg: 18:24 Ank: 18:28	Mot: Opalatorget



Used an Algorithm Today?

# Used an algorithm today?

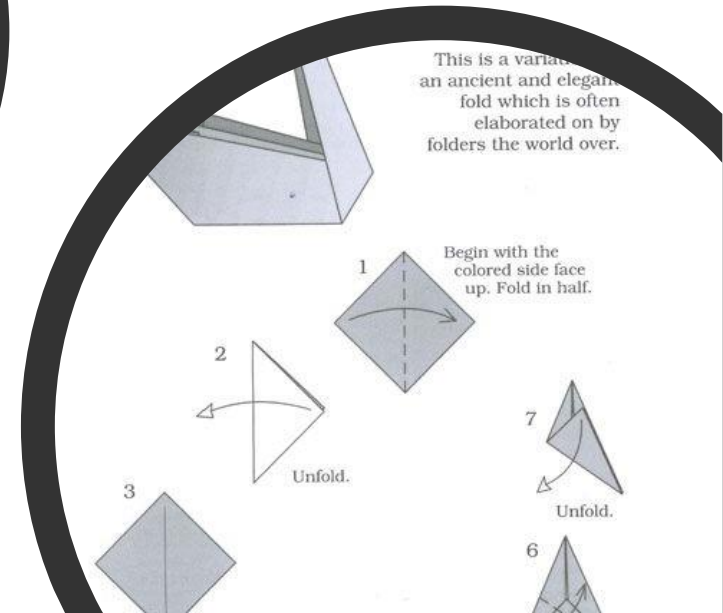
- Bake a cake
- Google translate
- Internet banking
- Google search
- Origami Swan



Used an algorithm today?



FTFTALILL-AVAV  
--FTAL-LLAAV--



# What is an Algorithm?

*A set of steps that defines how a task is performed.*

*An algorithm is an ordered set of unambiguous, executable steps that defines a terminating process.*

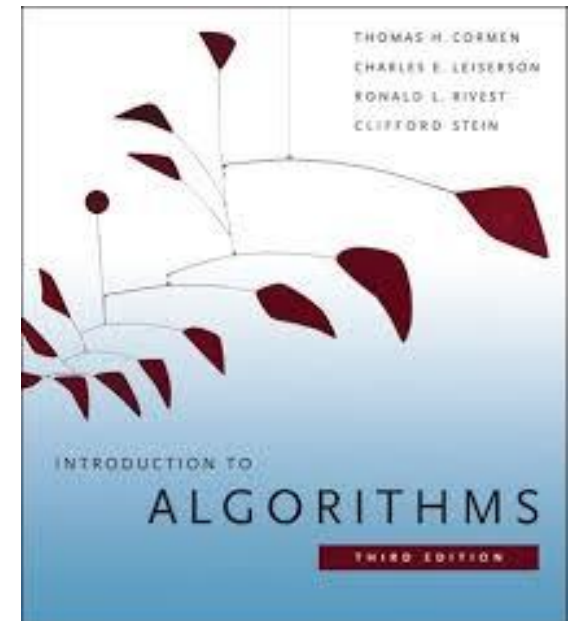
*Brookshear*

# What is an Algorithm?

*An Algorithm is a well-defined computational procedure that takes some value, or a set of values, as input and produces some value, or set of values as output.*

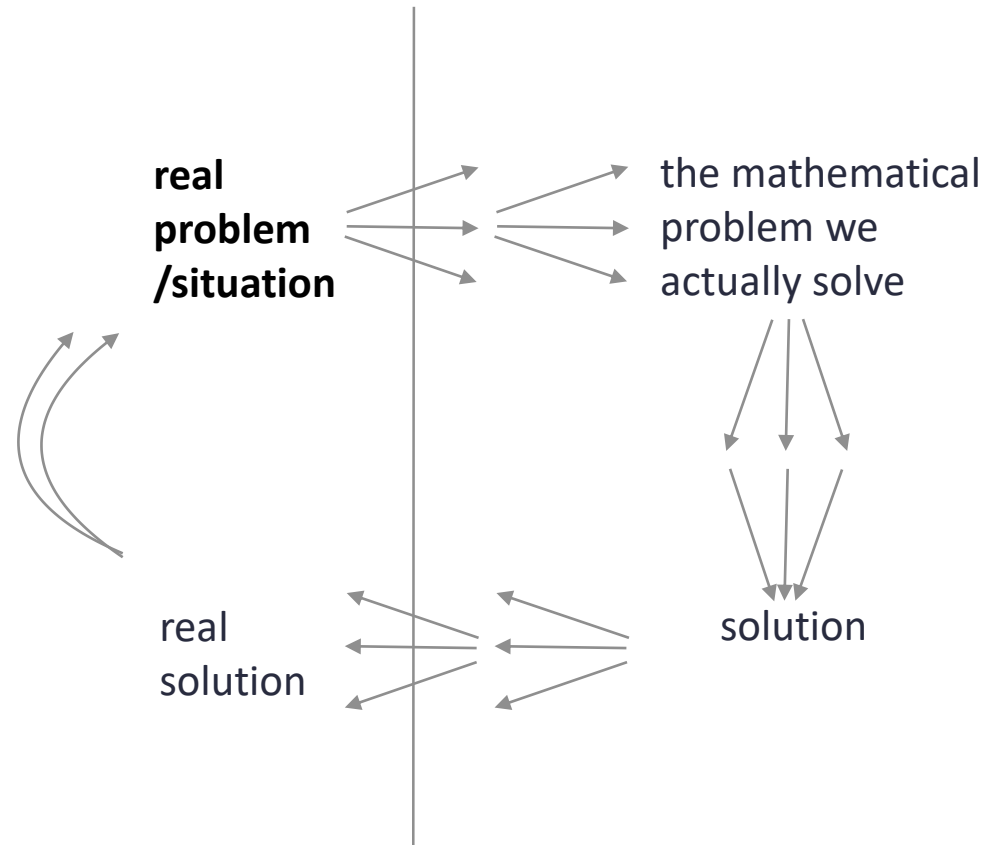
*An algorithm is thus a sequence of computational steps that transform input into output.*

- More formal definition uses Turing machines





# Algorithms in relation to modelling and problem solving



*An iterative and creative design process!*



# First Known Algorithm?

- Greatest common divisor (GCD) algorithm by Euclid  
ca 300 B.C.

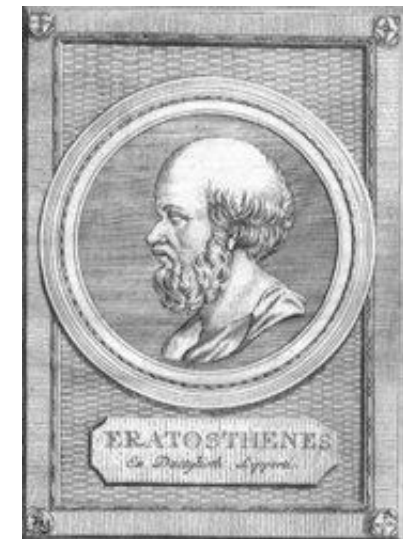
*Euclid's Elements*

- Prime numbers: Sieve of Eratosthenes, ca 200 B.C.

Animations: (sorting and prime numbers)

<https://www.youtube.com/watch?v=ZZuD6iUe3Pc>

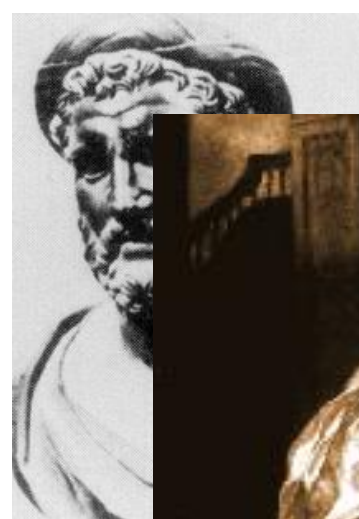
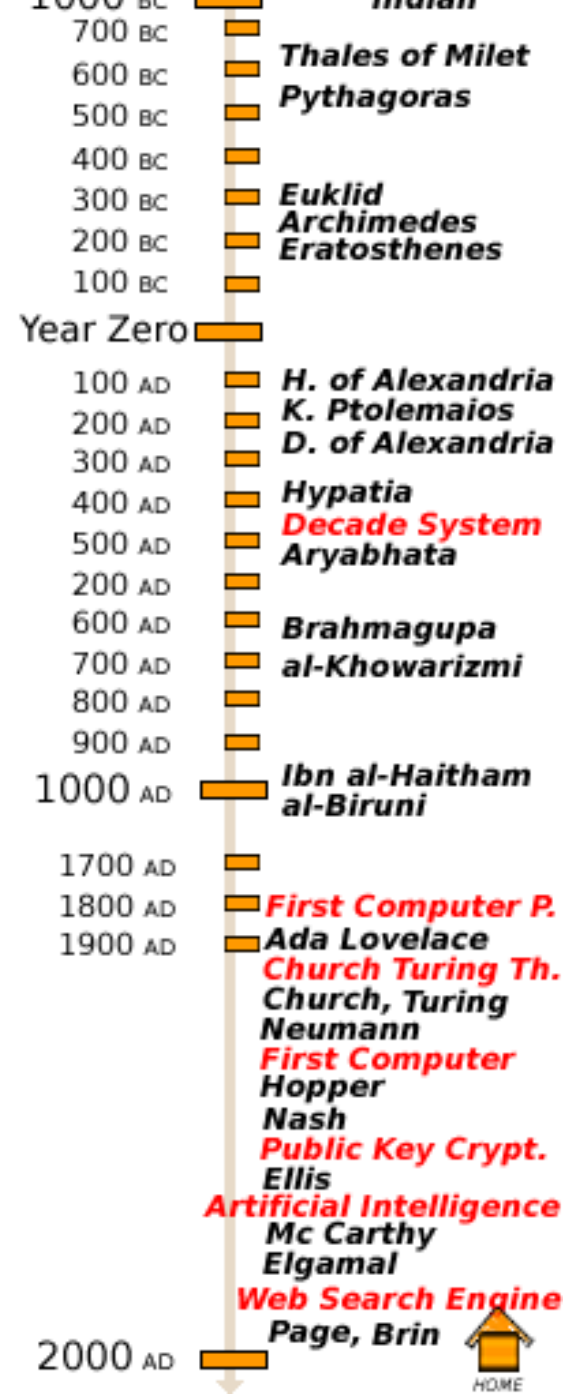
[https://en.wikipedia.org/wiki/Sieve\\_of\\_Eratosthenes](https://en.wikipedia.org/wiki/Sieve_of_Eratosthenes)



# Sieve of Eratosthenes

	2	3	4	5	6	7	8	9	10	Prime numbers
11	12	13	14	15	16	17	18	19	20	
21	22	23	24	25	26	27	28	29	30	
31	32	33	34	35	36	37	38	39	40	
41	42	43	44	45	46	47	48	49	50	
51	52	53	54	55	56	57	58	59	60	
61	62	63	64	65	66	67	68	69	70	
71	72	73	74	75	76	77	78	79	80	
81	82	83	84	85	86	87	88	89	90	
91	92	93	94	95	96	97	98	99	100	
101	102	103	104	105	106	107	108	109	110	
111	112	113	114	115	116	117	118	119	120	

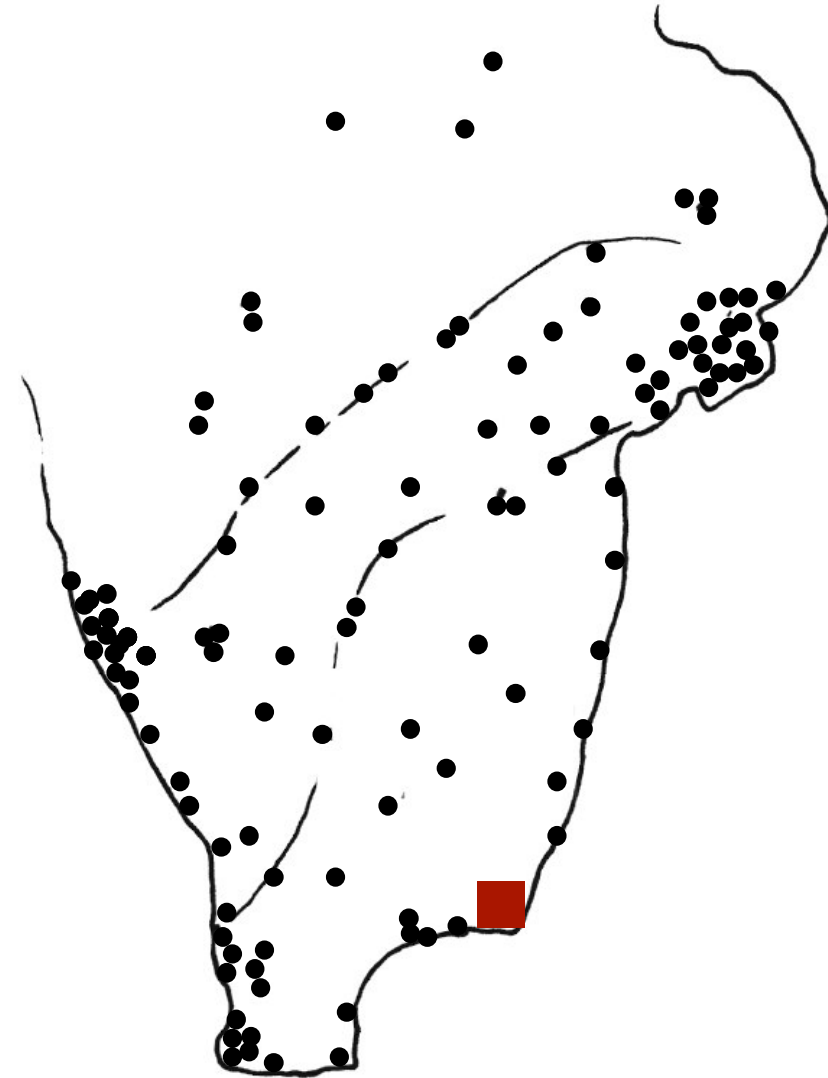
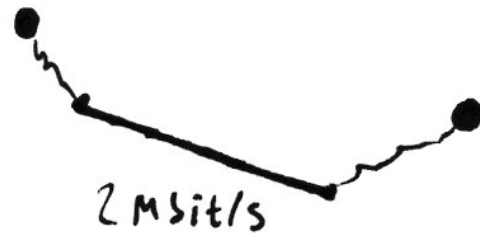
# Some History



# Telephone operator problem (real applied problem)

A Swedish mobile phone operator needs to connect all base station to its main switch.

How can we best rent communication lines from the national fixed network?



# The Shortest Path Problem

The screenshot shows the Västtrafik website's 'Reseplaneraren' (Route Planner) interface. The search criteria are: **Sök resa: Korvågen, GÖTEBORG (Hållplats) - Opalltorget, GÖTEBORG (Hållplats) (torsdag 16 oktober 2008)**. The results table shows the following data:

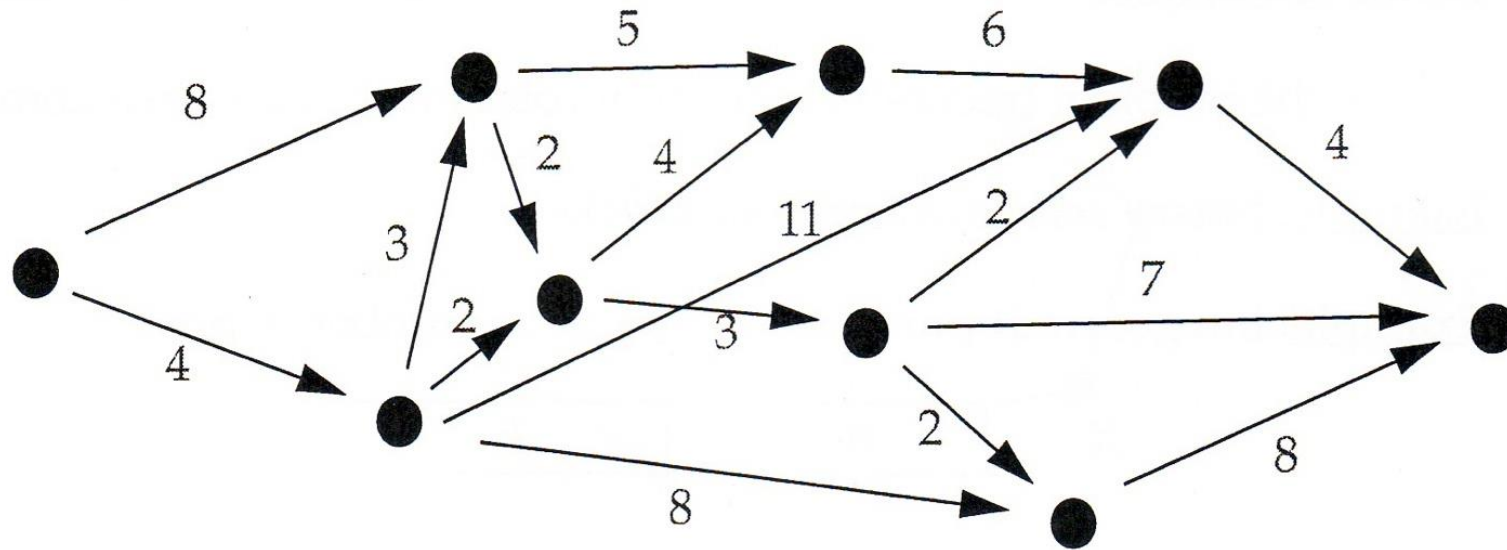
Avgång	Ankomst	Rasttid	Bytan	Trafikslag
<input type="checkbox"/> 17:50	18:19	00:29	1	Spårvagn 8, Spårvagn 7
<input checked="" type="checkbox"/> 17:59	18:28	00:29	1	Spårvagn 8, Spårvagn 7
<input type="checkbox"/> 18:08	18:38	00:30	1	Spårvagn 8, Spårvagn 7
<input type="checkbox"/> 18:25	18:49	00:24	0	Spårvagn 8
<input type="checkbox"/> 18:31	19:02	00:31	1	Spårvagn 8, Spårvagn 7
<input type="checkbox"/> 18:35	19:07	00:32	1	Spårvagn 8, Spårvagn 1

Below the table, there is a section for 'Detajerad resväg: Korvågen - Opalltorget (torsdag 16 oktober 2008)' with a table showing line details:

Linje	Från/Till	Tid	Information
Spårvagn 8	Korvågen Läge F Frökunda Torg Läge B	Avg: 17:59 Ank: 18:19	Mot: Frökunda Torg
Spårvagn 7	Frökunda Torg Läge B Opalltorget Läge B	Avg: 18:24 Ank: 18:28	Mot: Tynnered

How solve?

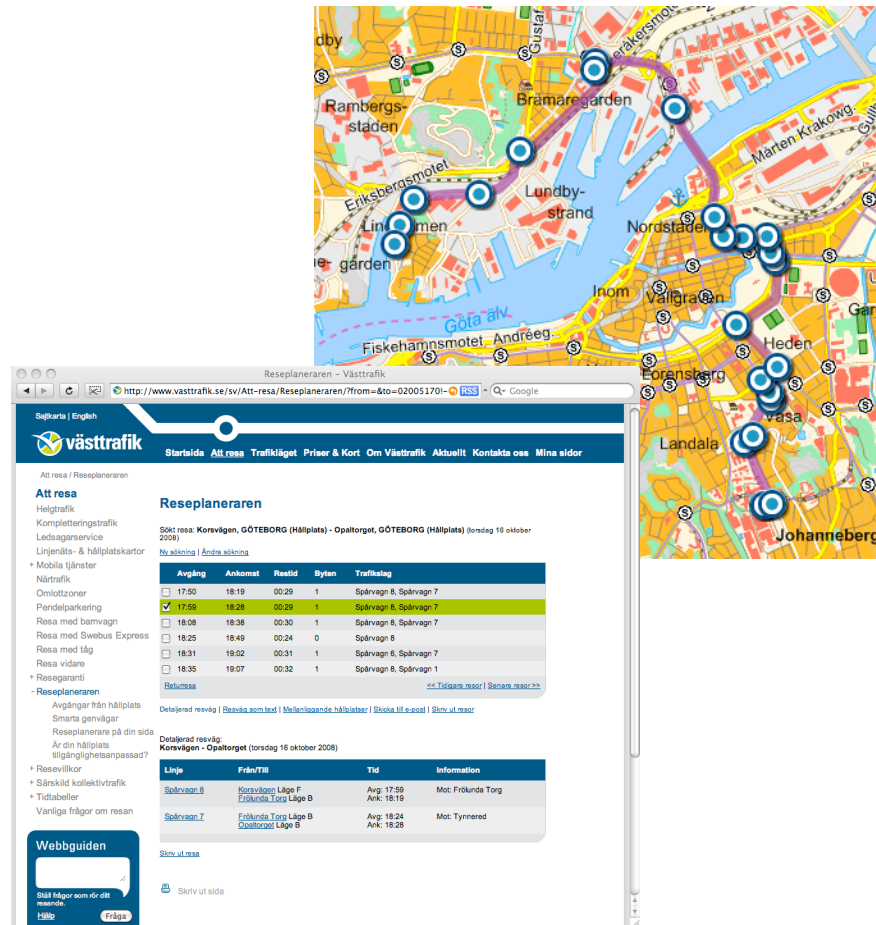
# Solving the directed shortest path problem with dynamic programming



Traverse nodes from left to right and mark with distance from origin. Dijkstra's algorithm 1956 .

Circumvents the combinatorial explosion!  
(not possible for all kinds of problems)

# The Shortest Path Problem



The image shows a screenshot of the Västtrafik website's route planner. At the top, there is a map of a city area with several blue circular markers representing stops. A purple line indicates a suggested route connecting these stops. Below the map, the website interface is visible, including a search bar and a list of travel options. The selected option is highlighted in green. The interface includes sections for 'Att resa', 'Reseplaneraren', and 'Webbguiden'.

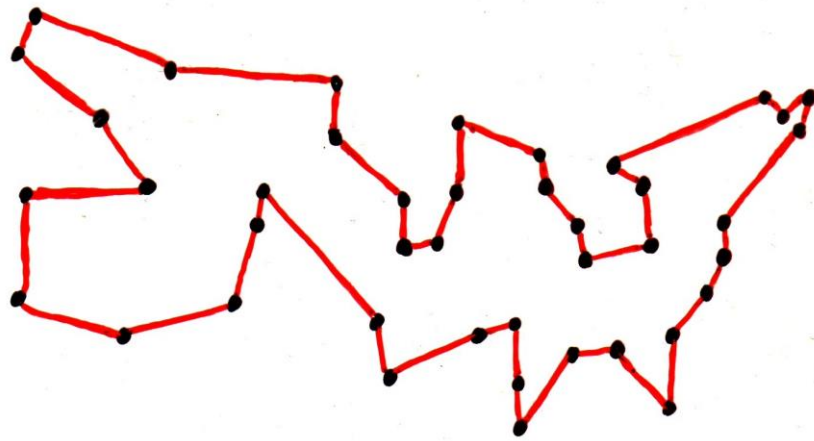
polynomial growth



n	$c n^2$
10	0,001 s
20	0,004 s
30	0,009 s
40	0,016 s
50	0,025 s
60	0,036 s



# The Travelling Salesperson Problem



no known polynomial algorithm!

exponential growth



$n$	$c 2^n$
10	0,001 s
20	1 s
30	18 min
40	13 days
50	36 years
60	36600 years

Why is TSP difficult? Reference and examples:

[https://www.google.com/url?sa=t&rct=j&q=&esrc=s&source=web&cd=11&ved=2ahUKEwiL6OP\\_iNjIAhURzaQKHcCeCHEQFjAKegQIAhAC&url=https%3A%2F%2Fpdfs.semanticscholar.org%2F7487%2F7695841673ece0e4782fdb88.pdf&usg=AOvVaw3914Eqq0wxHhc6vbw-c-gK](https://www.google.com/url?sa=t&rct=j&q=&esrc=s&source=web&cd=11&ved=2ahUKEwiL6OP_iNjIAhURzaQKHcCeCHEQFjAKegQIAhAC&url=https%3A%2F%2Fpdfs.semanticscholar.org%2F7487%2F7695841673ece0e4782fdb88.pdf&usg=AOvVaw3914Eqq0wxHhc6vbw-c-gK)

# TSP

## Sweden Tour

24,978 Cities

0 50 100 Kilometers  
0 50 100 Miles

Lambert Conformal Conic Projection, SP 47N/E24



Graphic Pairing Construction

Data	Plan	Rule	APC	Report	Options	Help	15:25							
Window	01/11	02/11	03/11	04/11	05/11	06/11	07/11	08/11	09/11	10/11	11/11	12/11	13/11	14/11
	01/11			02/11			03/11			04/11				
1 12 0/0/0/0/1/2	FRA	3 3	3	LIN	LIN	36 325 3251	FRA							
1 1 0/0/0/0/1/2	MUC	43 43 40 40	0-0 00	MUC										
1 12345 0/0/0/0/1/2	FRA	40	40 40 40	HAM		HAM 40 40 41 41	HAM		HAM 0	3726	ATH	ATH 373 380	IST	
1 123456 0/0/0/0/1/2	FRA	2	4 4 4 4	DUS		DUS 4 4 4 4	DUS		DUS 4 4 4 4	DUS	DUS	DUS 4 4 4 4	DUS	
1 123456 0/0/0/0/1/2	FRA	0	40 40	HAJ		HAJ 40 40 41 41	HAJ		HAJ 40 40 41 41	HAJ	HAJ	HAJ 40 40 41 41	HAJ	
1 12 0/0/0/0/1/2	FRA	31 31	3210	SVO	SVO	3213 481 470	FRA							
1 12356 0/0/0/0/1/2	FRA	3210	0005	GVA	GVA	46 4	BRU		BRU 4	36 3	NAP			
1 12 0/0/0/0/1/2	MUC	40 40	3	BUD	BUD	33 33 3	MUC							
1 12345 0/0/0/0/1/2	FRA	3 34	3816	IST	IST	380 373	ATH	ATH 3723 3846	IST			IST 380 373	ATH	
1 12 0/0/0/0/1/2	FRA	4 4 4		GVA	GVA	46 006S	FRA							
1 12 0/0/0/0/1/2	FRA	4 4 4		CDG	CDG	4 007S	FRA							
1 123 0/0/0/0/1/2	FRA	3 35 4		BRU	BRU	4 3 3 4	BRU	BRU 4 4816 4901	FRA					
1 123456 0/0/0/0/1/2	FRA	3846	3847 0	HAM	HAM	40 40	HAM	HAM 40 40	HAM			HAM 40 40	HAM	
1 1 0/0/0/0/1/2	FRA	4 46	005	FRA										
1 123 0/0/0/0/1/2	FRA	3736	5-0	ATH	ATH	3723 3	LIN	LIN 36 325 3251	FRA					
1 1 0/0/0/0/1/2	FRA	4816 4901	10-45 45-10	FRA										
1 123 0/0/0/0/1/2	FRA	3 3 0		HAJ	HAJ	0 28 28 4	GVA	GVA 45 4 4	FRA					
1 1234 0/0/0/0/1/2	FRA	2 3230 3221		DUS	DUS	4 4 4 4	DUS	DUS 3230	SVO	SVO 3213 481 470	FRA			
1 123456 0/0/0/0/1/2	FRA	481 470	0-0 0-0	STR	STR	40 40	STR	STR 40 40	STR	STR 40 40	STR			
1 123456 0/0/0/0/1/2	FRA	33 3 8		DUS	DUS	4 4	DUS	DUS 4 4	DUS	DUS 4 4	DUS			
1 1 0/0/0/0/1/2	FRA	480 475	3 3	FRA										
1 1 0/0/0/0/1/2	FRA	325 3251		FRA										
1 1 0/0/0/0/1/2	FRA	341 341	4 45	FRA										
1 1 0/0/0/0/1/2	FRA	47 471	43 43	FRA										
1 123 0/0/0/0/1/2	MUC	35	05	NAP	NAP	3 35 4	GVA	GVA 45 3 3	MUC					

Assign value: 0/0/0/0/1/2. Crew filter: On  
 SVO - FRA LH 3211 -1 J 123.56. A320 LH3306 0 F000 C144 M000 1/0/1/0/0/1/2  
 Gnt : 1605 - 1920 GDOR 1 Date(GDOP): 931101 SSIX 320 area : EU LH LH  
 Local : 1905 - 2020 Crew comp: booked:0/0/0/0/1/2

931101 - 931114 : READY  
 A320Nov01No cabl4\_scrat MTV  
 352 rows. Dated CBRs 931101 - 931104  
 0 931101 - 931114

## The resulting optimization problem

$$\begin{aligned} \text{minimize} \quad & 2x_1 + 2x_2 + 2x_3 + 2x_4 + x_5 + x_6 + x_7 + x_8 + 2x_9 + 2x_{10} \\ & + 2x_{11} + 2x_{12} + 2x_{13} + 2x_{14} + 2x_{15} + 2x_{16} + 2x_{17} \end{aligned}$$

subject to

$$x_1 + x_2 + x_3 + x_4 + x_9 + x_{10} = 1$$

$$x_1 + x_2 + x_3 + x_4 + x_9 + x_{10} = 1$$

$$x_2 + x_5 + x_6 + x_8 + x_{11} + x_{12} + x_{13} + x_{14} + x_{15} = 1$$

$$x_2 + x_3 + x_5 + x_8 + x_{11} + x_{13} + 2x_{14} + 2x_{15} + x_{16} + x_{17} = 1$$

$$x_3 + x_4 + x_7 + x_8 + x_{10} + x_{13} + x_{14} + 2x_{15} + x_{16} + 2x_{17} = 1$$

$$x_4 + x_6 + x_7 + x_8 + x_{10} + x_{12} + x_{13} + x_{15} + x_{17} = 1$$

$$x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8, x_9, x_{10}, x_{11}, x_{12}, x_{13}, x_{14}, x_{15}, x_{16}, x_{17} \in \{0, 1\}$$

**PAROS**



Prereq: Math &  
data structure

# Courses and Programs

Core:

- *Algorithms* TIN093/DIT602
- Algorithms, advanced TDA251/DITDIT281

Related:

- Algorithms for Machine learning and inference TDA231/DIT380
- Applied Machine learning DAT340/DIT866
- Discrete optimization TDA206/DIT370
- *Mathematical modelling and problem solving*, Applied mathematical thinking

CS bachelor  
and master  
(GU)

"CS-all" (MPALG)  
master (CTH)

Data  
science and  
AI master  
(CTH)

Applied data  
science master  
(GU)

# More Courses

- *Introduction to data science and AI* DAT405 (new)
- Techniques for large scale data DAT345/DIT871
- Design of AI systems (new)
- Computational methods for bioinformatics TDA507/DIT741
- Natural language processing with machine learning (new)
- Bachelor thesis and master's thesis projects
- Project course and seminar course

# Research Areas within the Division DSAI

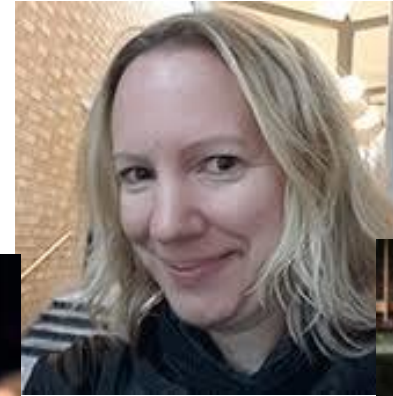
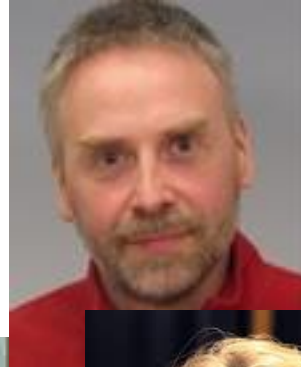
***Machine learning***, Artificial intelligence, Bioinformatics, ***Algorithms***, Graph theory, Randomized algorithms, Combinatorial optimization, Natural Language processing, Reinforcement learning, Unsupervised learning, Neural networks, Self-driving cars, Applications of machine learning in health, ***Mathematical modelling*** ...

Talks earlier in  
this seminar  
series

<https://www.chalmers.se/en/departments/cse/organisation/ds/Pages/default.aspx>

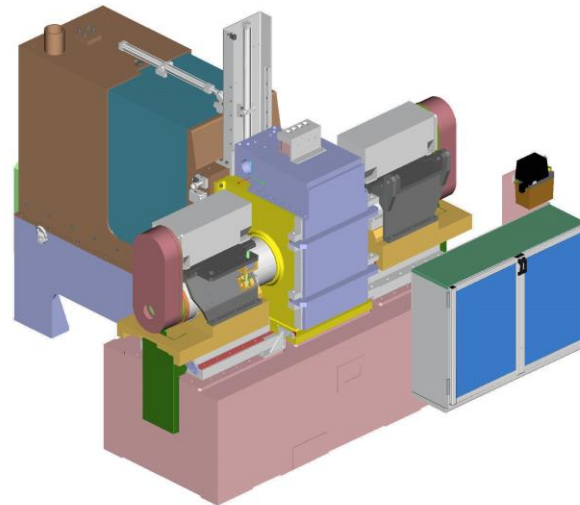
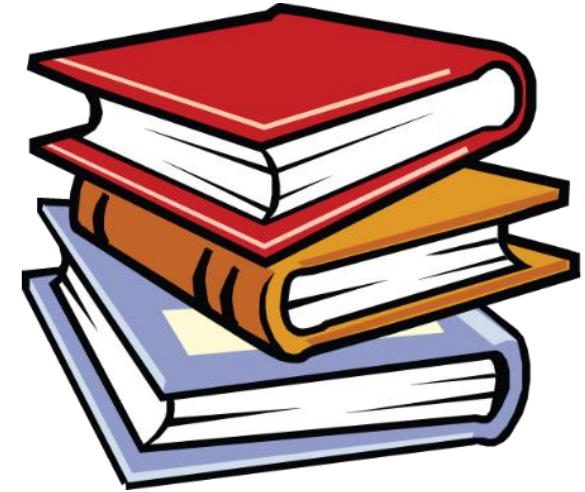


# Division Data science and AI



Graham Kemp, Alexander Schliep, Dag Wedelin, Birgit Grohe, *Ashkan Panahi*,  
Christos Dimitrakakis, Devdatt Dubhashi, Richard Johansson, Claes Strannegård, *Fredrik Johansson*  
Morteza Chehregani, Peter Damaschke (+Phd students and postdocs)

# Algorithms Courses – What's in it?



# Course Content – Algorithms Toolbox

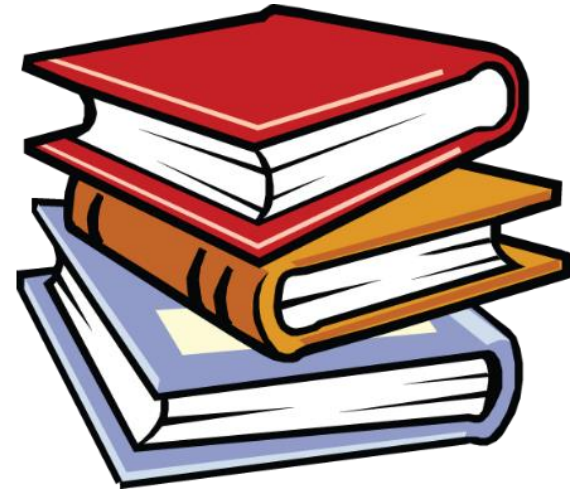
## *Algorithm design principles*

- Greedy
- Divide and Conquer
- Dynamic Programming
- Complete Search
- Heuristics
- ...



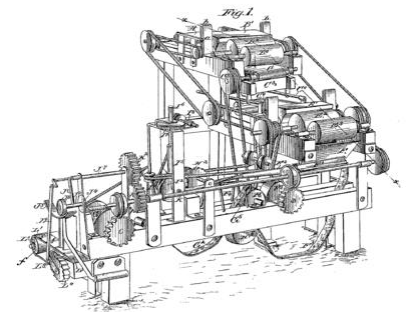
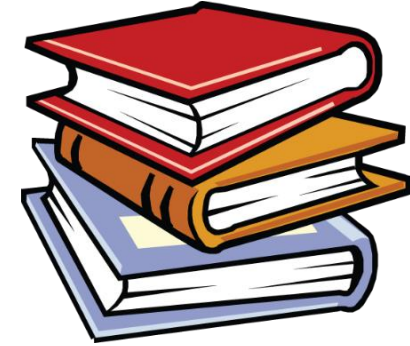
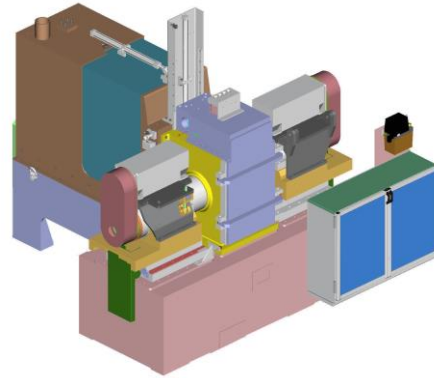
# Course Content: Standard Problems

- Searching
- Sorting
- Finding shortest path (SP)
- Finding longest path
- Max flow problem
- Travelling salesperson problem (TSP)
- Graph Coloring
- Satisfiability problem (SAT)
- ...



# Course Content: Standard Algorithms

- Binary Search
- Insertion Sort, Quicksort ...
- Breadth first search ...
- Dijkstras Algorithm
- Floyd Warshall Algorithm
- Ford Fulkerson Algorithm
- ...
- ...
- Randomized Algorithm for Scheduling Multi-Resource Jobs in the Cloud?





## *Good Algorithms?*

---

”[...] We want *good* algorithms in some loosely defined aesthetic sense. One criterion is the length of the time to perform the algorithm [...] Other criteria are adaptability of the algorithm to computers, its simplicity and elegance etc ”

Knuth 1973:3